

Mark Scheme (Results)

Summer 2016

Pearson Edexcel GCE in Statistics S1 (6683/01)

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# **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

#### PEARSON EDEXCEL GCE MATHEMATICS

# **General Instructions for Marking**

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
- **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M)
  marks have been earned.
- **B** marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

### 3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{\phantom{a}}$  will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- \* The answer is printed on the paper or ag- answer given
- L or d... The second mark is dependent on gaining the first mark

- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.
- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
  - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
  - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

# June 2016 6683 STATISTICS 1 Mark Scheme

Question Number	Scheme	Marks
1.(a)	$S_{dw} = 13833 - \frac{"1960" \times 33.6}{8}$ or $13833 - \frac{65856}{8}$ (But $13833 - 8232$ is M0) = $\underline{5601}$ (*)	M1 A1 cso
(b)	w, since the number of wiggles depends on the distance or $w$ depends on $d$	B1 (2) (1)
(c)	$r = \frac{5601}{\sqrt{394600 \times 80.481}}, = 0.99389$ awrt <u>0.994</u>	M1,A1
(d)	$b = \frac{5601}{394600}$ , = 0.014194 (awrt 0.014)	(2) M1, A1
	$a = \frac{33.6}{8} - 0.01419 \times \frac{1960}{8} = 4.2 - 0.01419 \times 245 = 0.72244$ $w = 0.722 + 0.0142d$	M1 A1
(e)	(i) [0.722 + 0.0142×350 = ] <b>awrt: <u>5.7</u></b> or <u>5.6</u> (ii) Reliable since 350 m is in the range of the data	(4) B1 B1 (2) [11 marks]
	Notes	[II IIIIII]
(a)	M1 for clear attempt to find $\Sigma d$ and use in a correct formula. Accept 130 For the M1 we can condone a single slip e.g. using 1383 instead of 13 A1cso for correct $\Sigma d$ and 5601 only. Must see the formula and so have sco	833 etc
(b)	B1 Must select w (or wiggles) and reason based on the idea that w is dependent on d Allow w "changes according to"/ "is determined/affected by" Must mention w and d B0 for "w is measured" or "d is explanatory/indep't" or "w can't be controlled" or "w responds to d"	
(c)	M1 for a correct expression (Allow ft of their incorrect $S_{dw}$ ) A1 for awrt 0.994 (Answer only 2/2) [Answer only of 0.99 scores M1A	<b>\</b> 0]
(d)	$1^{\text{st}}$ M1 for a correct expression for $b$ . (Allow ft of their incorrect $S_{dw}$ ) $1^{\text{st}}$ A1 for awrt 0.014 No fractions. [Answer only 2/2] Can be given at final equation. [Must come from correct formula <u>not</u> gradient of line from e.g. (650, 9.555) to (30, 0.725)] $2^{\text{nd}}$ M1 for a correct method for $a$ . Follow through their value of $b$ and their $\Sigma d$ $2^{\text{nd}}$ A1 for a correct equation for $w$ and $d$ with $a$ = awrt 0.722 and $b$ = awrt0.0142 No fractions Equation in $x$ and $y$ is A0 Answer only 4/4	
(e)	1 <sup>st</sup> B1 for awrt 5.7 or awrt 5.6 2 <sup>nd</sup> B1 for a reason citing 350 (m) or mentioning <i>d</i> is in the range of the dareliable. Allow "Interpolation (or not extrapolation) therefore reliables aying "5.7 (or <i>w</i> or just "it") is in the range" is B0 "accurate" instead of "reliable" is correlation" (without mention of interpolation o.e.) is B0 Apply ISW if a correct content of the second of the sec	able". s B0 "strong

Question Number	Scheme	Marks
2.(a)	p + q + 0.2 + 0.3 + p = 1 or $2p + q = 0.5$ (o.e.)	B1
(b)	$[E(X) =] -2p - q + \frac{1}{2} \times 0.2 + \frac{3}{2} \times 0.3 + 2p = 0.4] \underline{\text{or}} -q + 0.1 + 0.45 = 0.4]$ $\underline{q = 0.15}$	M1A1 A1
(c)	2p + ``0.15'' = 0.5  (o.e) $p = 0.175$	(3) M1 A1 (2)
(d)	$[Var(X) =] 2.275 - (0.4)^2$ = 2.115 (Accept 2.12)	M1 A1 (2)
(e)		M1 dM1
	$= 0.6 - q = 0.45 \text{ (or } \frac{9}{20})$	A1ft
( <b>f</b> )( <b>i</b> )	S > R when $x = 1.5$ and 2 $P(Sarah wins) = 0.3 + p = 0.475$ (or $\frac{19}{40}$ )	(3) M1 A1ft
(ii)	$R > S$ when $x = -2$ and $\frac{1}{2}$ or $r = -\frac{1}{2}$ and 2	M1
	P(Rebecca wins) = $0.2 + p = 0.375$ (or $\frac{15}{40}$ )	A1ft (4) [15 marks]
	Notes	
(a) (b)	B1 for any correct equation based on sum of probs. = 1  Correct answer only in (b), (c), (d), (e) or (f) scores full marks for t  M1 for an attempt at an expression based on E(X). At most 2 errors or om  1 <sup>st</sup> A1 for a correct equation [May be implied by a correct answer]  2 <sup>nd</sup> A1 for $q = 0.15$ or exact equivalent e.g. $\frac{6}{40}$	_
(c)	M1 for correct equation or using their equation from (a) with their $q$ , provided for $p = 0.175$ or exact equivalent e.g. $\frac{7}{40}$	vided $q \in [0,1]$
(d)	M1 for a correct numerical expression <u>but</u> M0 if followed by division by $k$ (e.g. $k = 5$ ) A1 for 2.115 or accept awrt 2.12 (also accept exact equivalent e.g. $\frac{423}{200}$ )	
(e)	1 <sup>st</sup> M1 for correct values for $R$ , allow 1 error, and allow unsimplified. Condone no label if not used as probabilities. If seen in table on QP allow, but <u>must</u> be labelled. Just writing the sum $\Sigma r$ is M0 but adding later can score 1 <sup>st</sup> M1 dependent on 1 <sup>st</sup> M1 for an attempt at an expression based on $E(R)$ , ft $p$ and $q$ , (if probabilities) ft their $r$ values. At least 3 correct (or correct ft) products seen. A1ft for 0.45 or (0.6 – their $q$ ) provided $q$ is a probability <b>Answers for (f) must be clearly labelled or take 1<sup>st</sup> as (i) and 2<sup>nd</sup> as (ii)</b>	
(f)(i)	M1 for identifying the correct values of $X$ A1ft for 0.475 or 0.3 + their $p$ , provided answer is a probability	
(ii)	M1 for identifying the correct values of $X$ or $R$ A1ft for 0.375 or 0.2 + their $p$ or 1 – their 0.475 – their $q$ , provided ans.	
SC1 X <sub>1</sub> ,X <sub>2</sub> SC2 swap Epen	They use two values of X: (i) for $P(S > R) = 0.445$ (B1) (ii) for $P(R > S) = 0.445$ (B1) (ii) for $P(R > S) = 0.475$ (B1) On epen record SC1 as: (i) M0A1 (ii) M0A1 and SC2 as M0A0	625 (B1). No ft ) No ft

Question Number	Scheme	Marks
3.(a)		
	$\left[\sigma_x^2 = \frac{985.88}{8} - \left(\frac{86.8}{8}\right)^2 = \frac{985.88}{8} - 10.85^2$	M1
	$\sigma_{x} = \sqrt{\frac{985.88}{8} - \left(\frac{86.8}{8}\right)^{2}} = \sqrt{123.235 - 117.7225} = \sqrt{5.5125}  \text{or}  \sqrt{\frac{44.1}{8}}$	A1
	= 2.3478 = awrt 2.35	A1 (3)
<b>(b)</b>	$S_{yy} = 8 \times \sigma_y^2 = 716 (3 \text{ sf}) \text{ but may see}$	
	$S_{yy} = 8 \times \sigma_y^2 = 716 \text{ (3 sf) but may see}$ $1136.584 - \frac{58^2}{8} \text{ or } 27628(.084168) - \frac{464^2}{8} \text{ or } 716.08 \text{ (= 716 to 3 sf) (*)}$	B1cso
	96.9464	(1)
(c)	$S_{xy} = 4900.5 - 58 \times 86.8$ or $4900.5 - \frac{86.8 \times 464}{8}$	M1
	= -133.9 (Allow -134)	A1
	122.0 /	(2)
(d)	$r = \frac{-133.9/8}{\sigma_x \times \sigma_y}$ or $\frac{-133.9}{\sqrt{44.1 \times 716}}$	M1
	= awrt $-0.753$ or $-0.754$	A1
(e)	r < 0 means high sunshine and low rain; this is high sunshine high rain	(2) B1
(6)	[this is not in keeping with the trend so] $r$ is closer to 0 or $ r $ decreases	B1
		(2)
	Notes	[10 marks]
(a)	M1 for a correct expr' for st. dev or variance (ignore label)[may be implied by 2	
	1 <sup>st</sup> A1 for a correct expression for st. dev (must have square root) can ignore	
	2 <sup>nd</sup> A1 for awrt 2.35 (allow $s = 2.5099$ or awrt 2.51). If they have $\sigma^2 = 2.3$ condone no label	35 score AU but
(b)	B1cso for a correct expression <u>or</u> sight of at least 716.08 (NB limits: 716 Do not allow verification. Beware circular arguments: $716 \rightarrow \Sigma y^2 \rightarrow$	
(c)	M1 for a correct expression for $S_{xy}$ (NB $\Sigma y = 464$ )	-
	A1 for $-133.9$ or awrt $-134$ [No fractions] (Answer only 2/2)	
(d)	M1 for a correct expression for $r$ (ft their values for $S_{xy}$ and $\sigma_x$ or $S_{xx}$ )[A	Allow ft of S,,,,1
(u)	A1 for awrt $-0.753$ or $-0.754$ (Answer only 2/2)	·- yy <b>1</b>
(e)	If they do not have an answer to (d) or their value of $r$ is > 0 or $ r $ > 1 so $1^{\text{st}}$ B1 for a suitable reason contradicting $r < 0$ e.g. new value is <u>not</u> in <u>keetor</u> both $14 > \overline{x}$ and $70 > \overline{y}$ or saying <u>both</u> above average. Allow for $-0.48 < 2^{\text{nd}}$ B1 for a correct statement about $r$ getting closer to zero e.g. $ r $ decreases A comment that $r$ decreases or $r$ is smaller or $r$ is "less negative" is " $r$ increases" is B0 <u>unless</u> they also say that it gets closer to 0	eping with trend $r < -0.47$

Question Number	Scheme	Marks
4.(a)	$[P(B \cap R') =]  \underline{0}$	B1
(b)	$P(B) = 0.27 + 0.33 = 0.6, \ P(D) = 0.27 + 0.15 + t \ , \ P(B \cap D) = 0.27$ $[P(B) \times P(D) = P(B \cap D) \text{ gives}] \qquad 0.6 \times (0.42 + t) = 0.27$	(1) M1 M1
	$0.42 + t = \frac{0.27}{0.6}$ or $0.6t = 0.018$	A1
	$t = \underline{0.03}$	A1 (4)
(c)	$[u=] 1-(0.6+0.15+t)$ $u = \underline{0.22}$	(4) M1 A1ft (2)
(d)(i)	$\left[\frac{P(D \cap R \cap B)}{P(R \cap B)} = \right] = \frac{0.27}{0.27 + 0.33}  \underline{\text{or}}  P(D \mid R \cap B) = P(D \mid B) = P(D)$	M1
	$= \underline{0.45}$	A1
(ii)	$\begin{bmatrix} P(D \cap [R \cap B']) \\ P(R \cap B') \end{bmatrix} = \begin{bmatrix} 0.15 \\ 0.15 + u \end{bmatrix}$	M1
	$=\frac{15}{37}$	A1
		(4)
(e)	$40 \times "0.45"$ and $37 \times "\frac{15}{37}"$	M1
	= <u>33</u>	A1 (2)
		(2) [13 marks]
	Notes	
(b)	1 <sup>st</sup> M1 for attempting 3 suitable probabilities, one involving $t$ (at least 2 core.g. sight of 0.6, 0.27, 0.42 + $t$ correctly labelled in terms of $B$ , $D$ , $R$ or in a co	rrect equation.
	$2^{\text{nd}}$ M1 for using the independence to form a linear equation in $t$ . ft their properties A1 for solving leading to a correct equation as far as $p + t = q$ or $pt = 2^{\text{nd}}$ A1 for 0.03 or exact equivalent	
(c)	M1 for a correct expression for $u$ . Allow their $t$ or just letter $t$ in a correct for 0.22 (or exact equivalent) or ft their $t$ . i.e. $u = 0.25 - t$ provided Can score M1A1ft provided their $u$ + their $t = 0.25$ where $u$ and $t$ are	u & t are probs
(d)(i)	M1 for a correct numerical ratio of probabilities	
(ii)	A1 for 0.45 or exact equivalent (Answer only 2/2) M1 for a correct numerical ratio of probabilities, ft their <i>u</i> , provided <i>u</i> is	a probability
	A1 for $\frac{15}{37}$ or $0.405$ or allow awrt 0.41 following a correct expression	-
(e)	M1 for a correct method for <u>both</u> 18 and 15 ft their 0.45 and their $\frac{15}{37}$ provided both in [0,1] NB P(D)×77 is M0 A1 for 33 only	
	NB $\frac{27}{33} \times 40 = 32.7$ which rounds to 33 but scores M0A0. (Ans only sen	d to review)

Question Number	Scheme	Marks
5.(a)	Width = $\underline{0.5}$ (cm) e.g 4 [cm <sup>2</sup> ] represents 8 babies or frequency densities are 8 and 34 Height = $\underline{17}$ (cm)	B1 M1 A1 (3)
(b)	$[Q_2 =] \{3\} + \frac{(25-9)}{(26-9)} \times 0.5, \text{ or } \{3.5\} - \frac{(25-24)}{(41-24)} \times 0.5 = \text{awrt } \underline{\textbf{3.47}} \text{ (allow } \frac{59}{17} \text{)}$	M1, A1 (2)
(c)(i)	$\sum_{x=1}^{\infty} f(x) = 1 \times 1 + 2.5 \times 8 + 3.25 \times 17 + 3.75 \times 17 + 4.5 \times 7 = 171.5, \ \overline{x} = \frac{171.5}{50} = (3.43) \ (*)$	B1cso
(ii)	$\sqrt{\frac{611.375}{50} - 3.43^2}$ ,= 0.680147 = awrt <b>0.680</b> (Accept 0.68)	M1, A1
(d)	$[P(W < 3) = P\left(Z < \frac{-0.43}{0.65}\right)] = P(Z < -0.6615)$	(3) M1
	$= 1 - 0.7454 \text{ (tables)}$ $= 0.2546 \text{ awrt } 0.254 \sim 0.255$	M1 A1 (3)
(e)	(b) and (c)(i) mean $\neq$ med or skew <u>or</u> mean <u>~</u> median or no skew <b>and</b> comment (d) = 0.254 or 0.255 compare data = 0.18 (or 12.7 compared with 9) 0.18 different from 0.25 so normal not good <u>or</u> 0.18 similar to 0.25 so normal is OK	B1 B1 dB1
(f)(i) (ii)	No change in mean (since weight is the same) s.d. will decrease (Extra value is at "centre" so data more concentrated) Both statements correct <u>and</u> correct reasons for <u>each</u>	(3) B1 B1 dB1 (3) [17 marks]
	Notes	[=:======
(a)	M1 for clear representation of area with frequency or height $\times$ width = 8.5 A1 for 17 (cm) [Must be clear it is height not frequency] (Ans only must sati	
(b)	M1 for $\frac{16}{17} \times 0.5$ or if using $n + 1$ for $\frac{16.5}{17} \times 0.5$ May see $-\frac{1}{17} \times 0.5$ if working A1 for awrt 3.47 (or $\frac{59}{17}$ ) [check from correct working] or (if using $(n + 1)$ for 3.48	
(c)(i)	B1cso for $\Sigma fx$ (at least 3 correct & no incorrect products seen) and correct $\frac{\sum}{50}$	$\frac{fx}{0}$ or $\frac{171.5}{50}$
(ii)	M1 for a correct expression including square root. Must use 3.43 no ft for awrt 0.680 (accept 0.68). Allow use of $s = \text{awrt } 0.687$ (Ans only 2/	(2)
(d)	$1^{\text{st}}$ M1 for an attempt to standardise with 3, 3.43 and 0.65. Allow $\pm$ and also u $2^{\text{nd}}$ M1 for $1-p$ where $0.74  NB calculator gives 0.7458665 Allow \pm and also u for awrt 0.254 or 0.255$	se of their sd
(e)	1 <sup>st</sup> B1 for a statement about mean/median <b>and</b> compatible comment about nor 2 <sup>nd</sup> B1 for statement comparing their (d) with data (sight of 0.18 or 12.7 and 9 3 <sup>rd</sup> dB1 dep on 2 <sup>nd</sup> B1 for conclusion about normal compatible with 2 <sup>nd</sup> statem	required)
(f)(i) (ii)	1 <sup>st</sup> B1 for no change in mean {send a correct argument for <u>decrease</u> to review} 2 <sup>nd</sup> B1 for s.d. decreases 3 <sup>rd</sup> dB1 dep on 1 <sup>st</sup> and 2 <sup>nd</sup> Bs for a correct reason for <u>both</u> mean <u>and</u> sd e.g. "new mean the same so within 1 s.d. of old mean"	}

Question Number	Scheme	Marks
6.(a)	[ $T \sim N (240, 40^2)$ require $P(T > 300)$ ]	
	$P\left(Z > \frac{300 - 240}{40}\right)$	M1
	=1-P(Z<1.5) or $1-0.9332$	M1
	= awrt <u><b>0.0668</b></u> or 6.68%	A1
	240	(3)
<b>(b)</b>	$[P(T < n) = 0.20 \Rightarrow] \frac{n - 240}{40} = -0.8416$ $n = \text{awrt } 206 \text{ minutes}$	M1 B1
	n = awrt  206  minutes	A1
		(3)
(c)	$[P(W < \mu - 30 \mid W < \mu) = ] \frac{P(W < \mu - 30)}{P(W < \mu)}$	M1
	$=\frac{1-0.82}{0.50}$	A1
	$= \underline{0.36}$	A1cao (3)
		[9 marks]
	Notes	_
(a)	$1^{\text{st}}$ M1 for standardising with 300, 240 and 40. May be implied by use of 1. $2^{\text{nd}}$ M1 for $1 - P(Z \le 1.5)$ i.e. a correct method for finding $P(Z \ge 1.5)$	5 Allow <u>+</u>
	$2^{\text{nd}}$ M1 for $1 - P(Z \le 1.5)$ i.e. a correct method for finding $P(Z \ge 1.5)$ e.g. $1 - p$ where $0.5 \le p \le 0.99$	
	A1 for awrt 0.0668 (Answer only 3/3)	
(1)		0.0
(b)	M1 for an attempt to standardise with 240, 40 and n and set = $\pm z$ (0.8 < $ z $ < B1 for $z = \pm 0.8416$ (or better) used as a z value. Do not allow for 1 – 0.8416	
	Calc gives $0.8416212$ [May be implied by awrt 206.34, give B1 as we	
	A1 for awrt 206 (can be scored for using a z value of 0.84 or even 0.85)	_
	Must follow from correct working but a range of possible z values are Ol	K
Ans only	If answer is awrt 206 score M1B0A1 (unless of course $z = 0.8416$ seen) but awrt 206.34 scores 3/3	
(c)	M1 for the correct ratio expression (Not $P([W < 30 - \mu] \cap [W < \mu])$ ) on nu	ımerator)
	Condone use of $Z$ instead of $W$ only if they later get a correct numerical ratio	
	However they may write $P\left(Z < \frac{-30}{\sigma}\right)$ etc which is of course fine	
Uge 4el-le	1 <sup>st</sup> A1 for a correct numerical ratio	allarry
Use tables	May see use of $z = 0.92$ or better (calc: $0.9153650$ ) or $\sigma = 32.6 \sim 32.8$	anow:
ALT	$1^{\text{st}} \text{ M1 for } \frac{P(Z < -0.92)}{P(Z < 0)} \text{ and } 1^{\text{st}} \text{ A1 for } \frac{1 - 0.8212}{0.5} \text{ or } \frac{0.1788}{0.5}$	
	$2^{\text{nd}}$ A1 for 0.36 or an exact equivalent e.g. $\frac{9}{25}$ (Answer only M1A1A0)	
	The final answer of 0.36 <u>must</u> come from exact values; 0.36 rounded from 0.	3576 etc is A0

